

Name:

## NetEcon final exam

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For each question, check all boxes corresponding to correct answers. There may be zero, one or several.

1. Consider a game with  $n$  users sharing the same communication link. Each user  $i$  chooses a non-negative consumption  $x_i$  and receives a utility  $u_i(x_i, x_{-i}) = f(x_i) - (x_1 + \dots + x_n) - p_i$  where  $f(\cdot)$  is an increasing concave function and  $p_i$  is the price for user  $i$ .
  - The social welfare is the sum of utilities of all users.
  - If  $p_i=0$  for each user  $i$ , the consumptions chosen by users at Nash equilibrium maximize the social welfare.
  - Social welfare is always maximal at Nash equilibrium.
  - Social welfare is maximized at Nash equilibrium if the price imposed to each user equals the externality that he imposed on the society.
2. An expert has a belief  $q$  about the weather: she believes it will be sunny with probability  $q$  and rain with probability  $1-q$  on the next day. She reports a prediction  $p$  (i.e., she announces "it will be sunny with probability  $p$  tomorrow") and she is rewarded according to a scoring rule called  $S(\cdot)$ .
  - For any scoring rule, the expert has an incentive to report truthfully her belief.
  - If  $S(\cdot)$  is the Brier or the logarithmic scoring rule, then it is strictly dominant for the expert to report her true belief.
  - If  $S(\cdot)$  is any proper scoring rule, then it is strictly dominant for the expert to report her true belief.
  - The logarithmic scoring rule is strictly proper.
3. Consider a 2-players attacker defender game. The attacker has 2 actions, attack (a) or not-attack (na) and the defender has 2 actions, monitor (m) or not monitor (nm). The payoffs are (with  $\alpha_c > 0$ ,  $\alpha_f > 0$ ,  $\alpha_s > 0$ ,  $\beta_c > 0$ ,  $\beta_s > 0$ ):

		defender	
		m	nm
attacker	a	$-\beta_c, \alpha_c$	$\beta_s, -\alpha_s$
	na	$0, -\alpha_f$	$0, 0$

- There is no pure strategy Nash equilibrium.
- All Nash equilibria are in pure strategy.
- This is a zero-sum game.
- At the Nash equilibrium, the probability that the attacker attacks depends only on the payoff parameters of the defender  $\alpha_c, \alpha_f, \alpha_s$ .

4. Auctions. We consider auctions with a single item, where there is one seller and there are  $n$  buyers with independent identically distributed private value.

- In a first-price auction, bidding truthfully is weakly dominant.
- In a second-price auction, bidding truthfully is weakly dominated.
- The expected revenue for the seller is strictly higher in a first-price auction than in a second price auction.
- The expected revenue for the seller is strictly smaller in a first-price auction than in a second price auction.